

微分積分学 II 自習用問題・解答

4 部分積分

問 4.1.

$$(1) A = \frac{3}{4}, B = \frac{1}{4}$$

$$(3) A = 1, B = -1, C = 1$$

$$(2) A = -1, B = 1, C = -2$$

$$(4) A = 1, B = -4, C = 3$$

問 4.2.

$$(1) \frac{1}{3} \cdot \frac{1}{x-1} - \frac{1}{3} \cdot \frac{1}{x+2}$$

$$(3) \frac{1}{x-1} + \frac{2}{x^2+2}$$

$$(2) \left(-\frac{2}{x} + \frac{3}{x^2} \right) + \frac{2}{x+1}$$

$$(4) \frac{1}{x+1} - \frac{1}{(x+1)^2} + \frac{1}{(x+1)^3}$$

問 4.3.

$$(1) \frac{3}{4} \log|x+2| - \frac{1}{4} \log|x-2|$$

$$(3) 2 \log|x-2| - \log|x-1|$$

$$(5) -2 \log|x| - \frac{3}{x} + 2 \log|x+1|$$

$$(7) \log|x-1| - \frac{1}{2} \log(x^2+1) + \arctan x$$

$$(9) \frac{2}{3} \log|x-1| - \frac{1}{3} \log(x^2+x+1)$$

$$(11) \log|x+1| + \frac{1}{x+1} - \frac{1}{2(x+1)^2}$$

$$(2) \frac{1}{3} \log|x-1| - \frac{1}{3} \log|x+2|$$

$$(4) -\log|x+2| + \log|x-1| + \frac{2}{x-1}$$

$$(6) \frac{2}{3} \log|x-1| + \frac{1}{3} \log|x+2| + \frac{3}{x+2}$$

$$(8) \log|x-1| + \sqrt{2} \arctan \frac{x}{\sqrt{2}}$$

$$(10) \log|x-1| - 4 \log|x-2| + 3 \log|x-3|$$

問 4.4. 次の不定積分を求めよ.

$$(1) \frac{1}{2}x^2 + x + \log|x-1|$$

$$(3) \frac{1}{2}x^2 + \log|x-1| - \log|x+1|$$

$$(2) \frac{1}{2}x^2 - x + 3 \log|x+1|$$

$$(4) x + 3 \log|x| + \frac{3}{x} - 4 \log|x+1|$$

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5 三角関数の分数式

問 5.1.

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|--------------------------------------|--|--|
| (1) $-\frac{1}{2} \cos(2x + 1)$ | (2) $\frac{1}{2}x + \frac{1}{4} \sin 2x$ | (3) $\tan x$ |
| (4) $\log(1 + \sin x)$ | (5) $-\log \sin x + \cos x $ | (6) $-\log \cos x $ |
| (7) $\frac{1}{4} \sin^4 x$ | (8) $-e^{\cos x}$ | (9) $\arctan(\sin x)$ |
| (10) $\frac{1}{3} \cos^3 x - \cos x$ | (11) $\frac{1}{2} \log \left \frac{\cos x - 1}{\cos x + 1} \right $ | (12) $\frac{1}{2} \log \left \frac{\sin x + 1}{\sin x - 1} \right $ |

問 5.2.

- | | | |
|-----------------------------------|--|---|
| (1) $\tan \frac{x}{2}$ | (2) $-\frac{2}{1 + \tan \frac{x}{2}}$ | (3) $\log \left \tan \frac{x}{2} \right $ |
| (4) $-\frac{1}{\tan \frac{x}{2}}$ | (5) $\log \left \tan \frac{x}{2} + 1 \right $ | (6) $\log \left \frac{\tan \frac{x}{2} - 1}{\tan \frac{x}{2} + 1} \right $ |

6 無理式の積分

問 6.1.

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|-------------------------------------|--|---------------------------------------|
| (1) $\frac{1}{3} \sqrt{(2x - 1)^3}$ | (2) $\frac{3}{4} \sqrt[3]{(2x - 1)^2}$ | (3) $-\frac{1}{3} \sqrt{(4 - x^2)^2}$ |
| (4) $-\sqrt{4 - x^2}$ | (5) $\arcsin \frac{x}{2}$ | (6) $\arcsin \frac{x - 2}{2}$ |

問 6.2.

- | | |
|---|---|
| (1) $\frac{2}{5} \sqrt{(x - 1)^5} + \frac{2}{3} \sqrt{(x - 1)^3}$ | (2) $2 \log(\sqrt{x - 1} + 1)$ |
| (3) $2\sqrt{x - 1} - 2 \log(\sqrt{x - 1} + 1)$ | (4) $\frac{1}{3} \sqrt{(x - 1)^3} + \sqrt{x - 1}$ |
| (5) $2 \arctan \sqrt{x - 1}$ | (6) $\sqrt{2} \arctan \sqrt{\frac{x - 1}{2}}$ |