

# 1 經濟数学入門 I (自習用問題・略解)

問題 1.1.

- |               |               |               |                 |
|---------------|---------------|---------------|-----------------|
| (1) $x^8$     | (2) $x^{15}$  | (3) $x^3y^6$  | (4) $x^{13}y^6$ |
| (5) $8x^3y^6$ | (6) $2x^7y^6$ | (7) $4x^2y^6$ | (8) $-2x^5y^7$  |

問題 1.2.

- |                       |                     |                     |                     |
|-----------------------|---------------------|---------------------|---------------------|
| (1) $x^3$             | (2) $\frac{1}{x^2}$ | (3) $\frac{2}{x^3}$ | (4) $\frac{x^3}{2}$ |
| (5) $\frac{x^3}{y^3}$ | (6) $y^2$           | (7) $\frac{5y}{4x}$ | (8) $\frac{3x}{2y}$ |

問題 1.3.

- |                               |                                  |
|-------------------------------|----------------------------------|
| (1) $2x - 6$                  | (2) $-x^2 + 3x$                  |
| (3) $2x^2 - 4x + 6$           | (4) $-x^2 + 2x - 3$              |
| (5) $x^3 - 2x^2 + 3x$         | (6) $-3x^4 + 6x^3 - 9x^2$        |
| (7) $2x^3y - 4x^2y^2 + 6xy^3$ | (8) $-3x^4y + 6x^3y^2 - 9x^2y^3$ |

問題 1.4.

- |   |                                       |
|---|---------------------------------------|
| (1) $x - 2 + \frac{3}{x}$                 | (2) $x + 3 - \frac{4}{x}$             |
| (3) $x^2 - 2x + 3 - \frac{4}{x}$          | (4) $x^2 + 3 - \frac{4}{x}$           |
| (5) $x - 2 + \frac{3}{x} - \frac{4}{x^2}$ | (6) $x + \frac{3}{x} - \frac{4}{x^2}$ |

## 2 經濟数学入門 I (自習用問題・略解)

### 問題 2.1.

(1)  $5x + 3y$

(3)  $11y$

(5)  $x^2 + 5x + 6$

(7)  $x^3 - 4x^2 + 7x - 6$

(9)  $-2x^2 + 2x - 3$

(2)  $x + 5y$

(4)  $-6x^2 - 14xy + 3y^2$

(6)  $x^2 - xy - 6y^2$

(8)  $x^6 - 1$

(10)  $-2x^2 - 2xy - y^2 + 4x - 2$

### 問題 2.2.

(1)  $x^2 + 5x + 6$

(3)  $x^2 - 16$

(5)  $6x^2 + x - 12$

(7)  $x^2 - xy - 6y^2$

(9)  $x^3 - 4x^2 + 7x - 6$

(2)  $x^2 - x - 12$

(4)  $x^2 - 8x + 16$

(6)  $4x^2 + 12x + 9$

(8)  $6x^2 + xy - 12y^2$

(10)  $x^6 - 1$

### 問題 2.3.

(1)  $x^2(2x^2 - 3)$

(3)  $x(2x^3 - 3x + 2)$

(5)  $3x^2y^3(y + 4x)$

(7)  $x^4y^2(5y - 9x)$

(9)  $2xy(2x^2 - 3xy + 6y^3)$

(2)  $-2x^3(x^3 - 2)$

(4)  $-2x^2(x^4 - 2x - 4)$

(6)  $2x^3y(2y + 3x)$

(8)  $3x^2y^4(y - 5x)$

(10)  $-x^3(4y^2 + 6xy - 3x^2)$

### 問題 2.4.

(1)  $(3x - 4)(9x - 4)$

(3)  $3x^2(3x - 4)^3(7x - 4)$

(5)  $4x^4(3x - 4)^2(6x - 5)$

(7)  $2x^4(3x - 4)^2(3x - 10)$

(2)  $x(3x - 4)^2(15x - 8)$

(4)  $2x^3(3x - 4)(9x - 8)$

(6)  $12x^2(3x - 4)^4(2x - 1)$

(8)  $-6x^2(3x - 4)^4(x + 2)$

### 3 經濟数学入門 I (自習用問題・略解)

#### 問題 3.1.

(1)  $x = 3$

(2)  $x = 3$

(3)  $x = 2$

(4)  $x = 2$

(5)  $x = -2$

(6)  $x = -\frac{2}{3}$

#### 問題 3.2.

(1)  $(x, y) = (3, 5)$

(2)  $(x, y) = (3, 5)$

(3)  $(x, y) = (2, -1)$

(4)  $(x, y) = (2, -1)$

(5)  $(x, y) = (-1, 2)$

(6)  $(x, y) = (-2, -1)$

(7)  $(x, y) = (4, 8)$

(8)  $(x, y) = (6, 2)$

(9)  $(x, y) = (5, 5)$

(10)  $(x, y) = (\frac{16}{3}, 4)$

#### 問題 3.3.

(1)  $(x + 2)(x + 3)$

(2)  $(x + 6)(x - 1)$

(3)  $(x - 1)(x - 5)$

(4)  $(x - 3)^2$

(5)  $(x + 4)(x - 4)$

(6)  $x(x - 16)$

(7)  $2(x + 2)(x - 6)$

(8)  $-3(x + 4)(x - 2)$

(9)  $x(x - 2)(x - 3)$

(10)  $-2x(x + 3)^2$

#### 問題 3.4.

(1)  $x = -2, -3$

(2)  $x = -6, 1$

(3)  $x = 1, 5$

(4)  $x = 3$

(5)  $x = -4, 4$

(6)  $x = 0, 16$

(7)  $x = -2, 6$

(8)  $x = -4, 2$

(9)  $x = 0, 2, 3$

(10)  $x = 0, -3$

問題 3.5.

$$(1) x = \frac{4}{3}, \frac{4}{9}$$

$$(3) x = 0, \frac{4}{3}, \frac{4}{7}$$

$$(5) x = 0, \frac{4}{3}, \frac{5}{6}$$

$$(7) x = 0, \frac{4}{3}, \frac{3}{10}$$

$$(2) x = 0, \frac{4}{3}, \frac{8}{15}$$

$$(4) x = 0, \frac{4}{3}, \frac{8}{9}$$

$$(6) x = 0, \frac{4}{3}, \frac{1}{2}$$

$$(8) x = 0, \frac{4}{3}, -2$$

問題 3.6.

$$(1) (x, y) = (1, 3), (2, 4)$$

$$(3) (x, y) = (2, 4), (-4, -2)$$

$$(5) (x, y) = (1, 3), (-3, -1)$$

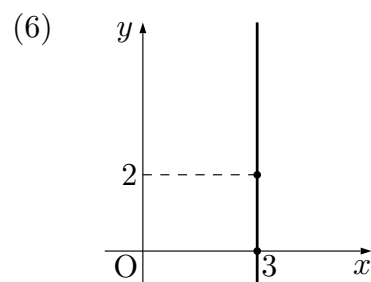
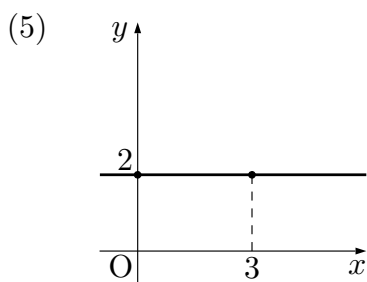
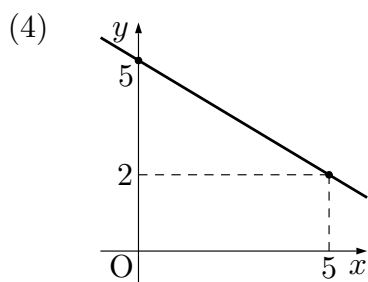
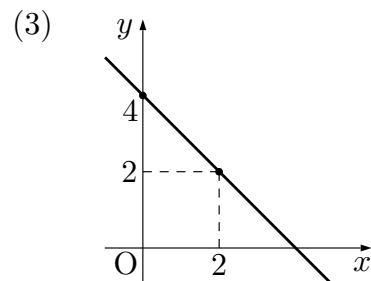
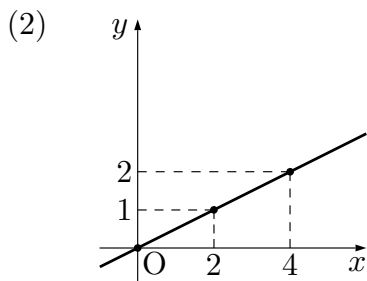
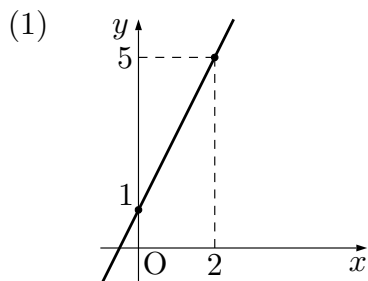
$$(2) (x, y) = (2, 3)$$

$$(4) (x, y) = (2, 3), (-3, -7)$$

$$(6) (x, y) = (4, 7)$$

## 4 經濟数学入門 I (自習用問題・略解)

### 問題 4.1.



### 問題 4.2.

(1)  $(x, y) = (2, 4)$

(2)  $(x, y) = (4, 2)$

(3)  $(x, y) = (2, 3)$

(4)  $(x, y) = (6, 7)$

(5)  $(x, y) = (6, 3)$

(6)  $(x, y) = (5, 2)$

### 問題 4.3.

(1)  $S = 6 \times 2 \times \frac{1}{2} = 6$

(2)  $S = 6 \times 4 \times \frac{1}{2} = 12$

(3)  $S = 8 \times 2 \times \frac{1}{2} = 8$

(4)  $S = 8 \times 6 \times \frac{1}{2} = 24$

(5)  $S = 5 \times 6 \times \frac{1}{2} = 15$

(6)  $S = 5 \times 5 \times \frac{1}{2} = \frac{25}{2}$

(7)  $S = 6 \times 3 \times \frac{1}{2} = 9$

(8)  $S = 3 \times 9 \times \frac{1}{2} = \frac{27}{2}$

### 問題 4.4.

(1)  $S = (6 + 3) \times 1 \times \frac{1}{2} = \frac{9}{2}$

(2)  $S = (6 + 3) \times 2 \times \frac{1}{2} = 9$

(3)  $S = (8 + 4) \times 1 \times \frac{1}{2} = 6$

(4)  $S = \left(8 + \frac{16}{3}\right) \times 2 \times \frac{1}{2} = \frac{40}{3}$

(5)  $S = \left(5 + \frac{10}{3}\right) \times 2 \times \frac{1}{2} = \frac{25}{3}$

(6)  $S = (5 + 1) \times 4 \times \frac{1}{2} = 12$

## 5 經濟数学入門 I (自習用問題・略解)

### 問題 5.1.

(1) 需要量 :  $D = 10$  , 供給量 :  $S = 2$

(2) 需要量 :  $D = 4$  , 供給量 :  $S = 4$

(3) 需要量 :  $D = 32$  , 供給量 :  $S = 12$

(4) 需要量 :  $D = 552$  , 供給量 :  $S = 32$

### 問題 5.2.

(1) 逆需要関数 :  $p = -q + 12$

(2) 逆需要関数 :  $p = -\frac{1}{4}q + 3$

逆供給関数 :  $p = q$

逆供給関数 :  $p = \frac{1}{2}q$

(3) 逆需要関数 :  $p = -\frac{1}{4}q + 10$

(4) 逆需要関数 :  $p = -\frac{1}{24}q + 25$

逆供給関数 :  $p = \frac{1}{6}q$

逆供給関数 :  $p = \frac{1}{16}q$

### 問題 5.3.

(1)  $p^* = 6$  ,  $q^* = 6$

(2)  $p^* = 2$  ,  $q^* = 4$

(3)  $p^* = 4$  ,  $q^* = 24$

(4)  $p^* = 15$  ,  $q^* = 240$

### 問題 5.4.

(1)  $CS = (12 - 6) \times 6 \times \frac{1}{2} = 18$

(2)  $CS = (3 - 2) \times 4 \times \frac{1}{2} = 2$

$PS = (6 - 0) \times 6 \times \frac{1}{2} = 18$

$PS = (2 - 0) \times 4 \times \frac{1}{2} = 4$

$TS = (12 - 0) \times 6 \times \frac{1}{2} = 36$

$TS = (3 - 0) \times 4 \times \frac{1}{2} = 6$

(3)  $CS = (10 - 4) \times 24 \times \frac{1}{2} = 72$

(4)  $CS = (25 - 15) \times 240 \times \frac{1}{2} = 1200$

$PS = (4 - 0) \times 24 \times \frac{1}{2} = 48$

$PS = (15 - 0) \times 240 \times \frac{1}{2} = 1800$

$TS = (4 - 0) \times 24 \times \frac{1}{2} = 120$

$TS = (25 - 0) \times 240 \times \frac{1}{2} = 3600$

(5)  $CS = (10 - 7) \times 12 \times \frac{1}{2} = 18$

(6)  $CS = (25 - 20) \times 120 \times \frac{1}{2} = 300$

$PS = (7 - 5) \times 12 \times \frac{1}{2} = 12$

$PS = \left(20 - \frac{25}{2}\right) \times 120 \times \frac{1}{2} = 450$

$TS = (10 - 5) \times 12 \times \frac{1}{2} = 30$

$TS = \left(25 - \frac{25}{2}\right) \times 120 \times \frac{1}{2} = 750$

## 6 経済数学入門 I (自習用問題・略解)

### 問題 6.1.

(1) 超過供給なので,  $q^{**} = 50 - 2 \times 15 = 20$

(2)  $CS = (25 - 15) \times 20 \times \frac{1}{2} = 100$

$$PS = \{(15 - 0) + (15 - 10)\} \times 20 \times \frac{1}{2} = 200$$

(3) 超過需要なので,  $q^{**} = 2 \times 5 = 10$

(4)  $CS = \{(25 - 5) + (20 - 5)\} \times 10 \times \frac{1}{2} = 175$

$$PS = (5 - 0) \times 10 \times \frac{1}{2} = 25$$

### 問題 6.2.

(1) 超過供給なので,  $q^{**} = 120 - 4 \times 15 = 60$

(2)  $CS = (30 - 15) \times 60 \times \frac{1}{2} = 450$

$$PS = \left\{ \left( 15 - \frac{5}{2} \right) + (15 - 10) \right\} \times 60 \times \frac{1}{2} = 525$$

(3) 超過需要なので,  $q^{**} = 8 \times 5 - 20 = 20$

(4)  $CS = \{(30 - 5) + (25 - 5)\} \times 20 \times \frac{1}{2} = 450$

$$PS = \left( 5 - \frac{5}{2} \right) \times 20 \times \frac{1}{2} = 25$$

### 問題 6.3.

(1) 
$$\begin{cases} q = 50 - 2p \\ q = 2p - 10 \end{cases}$$
 を解いて,  $p^\dagger = 15, q^\dagger = 20$

(2)  $CS = (25 - 15) \times 20 \times \frac{1}{2} = 100$

$$PS = (10 - 0) \times 20 \times \frac{1}{2} = 100$$

(3) 
$$\begin{cases} q = 50 - 2p \\ q = 2p - 30 \end{cases}$$
 を解いて,  $p^\dagger = 20, q^\dagger = 10$

$$(4) CS = (25 - 20) \times 10 \times \frac{1}{2} = 25$$

$$PS = (5 - 0) \times 10 \times \frac{1}{2} = 25$$

問題 6.4.

$$(1) \begin{cases} q = 120 - 4p \\ q = 8p - 60 \end{cases} \text{ を解いて, } p^\dagger = 15, q^\dagger = 60$$

$$(2) CS = (30 - 15) \times 60 \times \frac{1}{2} = 450$$

$$PS = \left(10 - \frac{5}{2}\right) \times 60 \times \frac{1}{2} = 225$$

$$(3) \begin{cases} q = 120 - 4p \\ q = 8p - 140 \end{cases} \text{ を解いて, } p^\dagger = \frac{65}{3}, q^\dagger = \frac{100}{3}$$

$$(4) CS = \left(30 - \frac{65}{3}\right) \times \frac{100}{3} \times \frac{1}{2} = \frac{1250}{3}$$

$$PS = \left(\frac{20}{3} - \frac{5}{2}\right) \times \frac{100}{3} \times \frac{1}{2} = \frac{625}{3}$$

$$(5) GS = \left(\frac{65}{3} - \frac{20}{3}\right) \times \frac{100}{3} = 500$$

$$TS = \left\{ \left(30 - \frac{5}{2}\right) + \left(\frac{65}{3} - \frac{20}{3}\right) \right\} \times \frac{100}{3} \times \frac{1}{2} = \frac{2125}{3}$$

$$(6) \text{ 課税前の均衡取引量は } q^* = \frac{220}{3}$$

$$\text{よって, 死荷重は } \left(\frac{65}{3} - \frac{20}{3}\right) \times \left(\frac{220}{3} - \frac{110}{3}\right) \times \frac{1}{2} = 300$$

問題 6.5.

$$(1) \text{ 課税後の供給関数は } q = \frac{3}{5} \left(p \div \frac{120}{100}\right) - 20 = \frac{1}{2}p - 20$$

$$\text{よって, } \begin{cases} q = 40 - \frac{1}{2}p \\ q = \frac{1}{2}p - 20 \end{cases} \text{ を解いて, } p^\dagger = 60, q^\dagger = 10$$

$$(2) CS = (80 - 60) \times 10 \times \frac{1}{2} = 100$$

$$PS = \left(50 - \frac{100}{3}\right) \times 10 \times \frac{1}{2} = \frac{250}{3}$$

$$(3) GS = (60 - 50) \times 10 = 100$$



$$(4) \text{ 課税後の供給関数は } q = \frac{3}{5} \left( p \div \frac{105}{100} \right) - 20 = \frac{4}{7}p - 20$$

$$\text{よって, } \begin{cases} q = 40 - \frac{1}{2}p \\ q = \frac{4}{7}p - 20 \end{cases} \text{ を解いて, } p^\dagger = 56, q^\dagger = 12$$

$$(5) CS = (80 - 56) \times 12 \times \frac{1}{2} = 144$$

$$PS = \left( \frac{160}{3} - \frac{100}{3} \right) \times 12 \times \frac{1}{2} = 120$$

$$(6) GS = \left( 56 - \frac{160}{3} \right) \times 12 = 32$$

### 問題 6.6.

$$(1) \text{ 支給後の供給関数は } q = 8(p + 5) - 100 = 8p - 60$$

$$\text{よって, } \begin{cases} q = 120 - 4p \\ q = 8p - 60 \end{cases} \text{ を解いて, } p' = 15, q' = 60$$

$$(2) CS = (30 - 15) \times 60 \times \frac{1}{2} = 450$$

$$PS = \left( 20 - \frac{25}{2} \right) \times 60 \times \frac{1}{2} = 225$$

$$(3) GS = -(20 - 15) \times 60 = -300$$

## 7 經濟数学入門 I (自習用問題・略解)

### 問題 7.1.

- (1) 2      (2) -1      (3)  $\frac{1}{3}$       (4) -0.8      (5) 0      (6) 0

### 問題 7.2.

- (1)  $2x$       (2)  $6x$       (3)  $6x^2$       (4)  $-12x^3$       (5)  $2x^3$       (6)  $-\frac{3}{5}x^5$

### 問題 7.3.

- (1)  $f'(x) = 2x - 3$       (2)  $f'(x) = -2x + 2$   
(3)  $f'(x) = x - 4$       (4)  $f'(x) = -\frac{1}{2}x - \frac{1}{3}$   
(5)  $f'(x) = 3x^2 - 4x + 3$       (6)  $f'(x) = -6x^2 + 6x - 4$   
(7)  $f'(x) = x^3 + x^2 + x + 1$       (8)  $f'(x) = \frac{1}{6}x^3 - \frac{1}{2}x^2 + x - 1$

### 問題 7.4.

- (1)  $f'(2) = 1$       (2)  $f'(2) = -2$   
(3)  $f'(2) = -2$       (4)  $f'(2) = -\frac{4}{3}$   
(5)  $f'(2) = 7$       (6)  $f'(2) = -16$   
(7)  $f'(2) = 15$       (8)  $f'(2) = \frac{1}{3}$

## 9 経済数学入門 I (自習用問題・略解)

### 問題 9.1.

(1)  $x = 4$

(2)  $x = 3$

(3)  $x = 2$

(4)  $x = -1$

(5)  $x = 1, 2$

(6)  $x = 2, -2$

(7)  $x = 3, -1$

(8)  $x = 6, -1$

### 問題 9.2.

(1)  $f''(x) = 2$

(2)  $f''(x) = \frac{2}{3}$

(3)  $f''(x) = -2$

(4)  $f''(x) = -4$

(5)  $f''(x) = 2x - 3$

(6)  $f''(x) = 6x$

(7)  $f''(x) = -2x + 2$

(8)  $f''(x) = -x + \frac{5}{2}$

### 問題 9.3.

(1)  $f''(3) = 2$

(2)  $f''(3) = \frac{2}{3}$

(3)  $f''(3) = -2$

(4)  $f''(3) = -4$

(5)  $f''(3) = 3$

(6)  $f''(3) = 18$

(7)  $f''(3) = -4$

(8)  $f''(3) = -\frac{1}{2}$

### 問題 9.4.

(1)  $x = 4$  のとき 極小

(2)  $x = 3$  のとき 極小

(3)  $x = 2$  のとき 極大

(4)  $x = -1$  のとき 極大

(5)  $x = 1$  のとき 極大  
 $x = 2$  のとき 極小

(6)  $x = -2$  のとき 極大  
 $x = 2$  のとき 極小

(7)  $x = 3$  のとき 極大  
 $x = -1$  のとき 極小

(8)  $x = 6$  のとき 極大  
 $x = -1$  のとき 極小

## 10 経済数学入門 I (自習用問題・略解)

### 問題 10.1.

(1) 極大値：なし

(2) 極大値：なし

(3) 極大値： $f(2) = 0$

(4) 極大値： $f(-1) = 8$

(5) 極大値： $f(1) = \frac{1}{6}$

(6) 極大値： $f(-2) = 16$

(7) 極大値： $f(3) = 5$

(8) 極大値： $f(6) = 12$

(9) 極大値： $f(4) = -4$

(10) 極大値： $f(-2) = 30$

(11) 極大値： $f(0) = 0$

(12) 極大値： $f(1), f(-1) = 1$

### 問題 10.2.

(1) 最大値： $f(0) = 6$

(2) 最大値： $f(-2) = \frac{19}{3}$

(3) 最大値： $f(2) = 0$

(4) 最大値： $f(0) = 6$

(5) 最大値： $f(3) = \frac{1}{2}$

(6) 最大値： $f(-2) = 16$

(7) 最大値： $f(3) = 5$

(8) 最大値： $f(3) = \frac{3}{4}$

(9) 最大値： $f(0) = 12$

(10) 最大値： $f(0) = 2$

(11) 最大値： $f(2) = 4$

(12) 最大値： $f(1), f(-1) = 1$

## 11 經濟数学入門 I (自習用問題・略解)

### 問題 11.1.

(1)  $C(2) = 16$ ,  $FC = 4$ ,  $VC(x) = x^2 + 4x$ ,  $VC(2) = 12$

(2)  $C(2) = 16$ ,  $FC = 6$ ,  $VC(x) = x^2 + 3x$ ,  $VC(2) = 10$

(3)  $C(2) = \frac{56}{3}$ ,  $FC = 4$ ,  $VC(x) = \frac{1}{3}x^3 + x^2 + 4x$ ,  $VC(2) = \frac{44}{3}$

(4)  $C(2) = 18$ ,  $FC = 6$ ,  $VC(x) = x^3 - 3x^2 + 8x$ ,  $VC(2) = 12$

### 問題 11.2.

(1)  $AVC(x) = x + 4$ ,  $AC(2) = 8$ ,  $AVC(2) = 6$ ,  $AFC(2) = 2$

(2)  $AVC(x) = x + 3$ ,  $AC(2) = 8$ ,  $AVC(2) = 5$ ,  $AFC(2) = 3$

(3)  $AVC(x) = \frac{1}{3}x^2 + x + 4$ ,  $AC(2) = \frac{28}{3}$ ,  $AVC(2) = \frac{22}{3}$ ,  $AFC(2) = 2$

(4)  $AVC(x) = x^2 - 3x + 8$ ,  $AC(2) = 9$ ,  $AVC(2) = 6$ ,  $AFC(2) = 3$

### 問題 11.3.

(1)  $MC(x) = 2x + 4$ ,  $MC(2) = 8$

(2)  $MC(x) = 2x + 3$ ,  $MC(2) = 7$

(3)  $MC(x) = x^2 + 2x + 4$ ,  $MC(2) = 12$

(4)  $MC(x) = 3x^2 - 6x + 8$ ,  $MC(2) = 8$

### 問題 11.4.

(1)  $R(x) = 10x$ ,  $MR(x) = 10$ ,  $\pi(x) = -x^2 + 6x - 4$ ,  $\pi(2) = 4$

(2)  $R(x) = 10x - x^2$ ,  $MR(x) = 10 - 2x$ ,  $\pi(x) = -2x^2 + 7x - 6$ ,  $\pi(2) = 0$

(3)  $R(x) = 12x$ ,  $MR(x) = 12$ ,  $\pi(x) = -\frac{1}{3}x^3 - x^2 + 8x - 4$ ,  $\pi(2) = \frac{16}{3}$

(4)  $R(x) = 12x - x^2$ ,  $MR(x) = 12 - 2x$ ,  $\pi(x) = -x^3 + 2x^2 + 4x - 6$ ,  $\pi(2) = 2$

## 12 経済数学入門 I (自習用問題・略解)

### 問題 12.1.

最適な生産量： $x^* = 2$

$$( R(x) = 12x - x^2, \pi(x) = -x^2 + 8x - 4, \pi(x^*) = 4 )$$

### 問題 12.2.

最適な生産量： $x^* = 4$

$$( R(x) = 10x - x^2, \pi(x) = -\frac{1}{3}x^3 + \frac{3}{2}x^2 + 4x - \frac{2}{3}, \pi(x^*) = 18 )$$

### 問題 12.3.

最適な生産量： $x^* = 3$

$$( R(x) = 18x - \frac{1}{2}x^2, \pi(x) = -x^3 - \frac{9}{2}x^2 + 54x - 72, \pi(x^*) = \frac{45}{2} )$$

### 問題 12.4.

最適な生産量： $x^* = 4$

$$( R(x) = 10x - 2x^2, \pi(x) = -\frac{1}{3}x^3 + \frac{5}{2}x^2 - 4x - \frac{1}{6}, \pi(x^*) = \frac{5}{2} )$$

### 問題 12.5.

最適な生産量： $x^* = 6$

$$( R(x) = 16x, \pi(x) = -x^2 + 12x - 4, \pi(x^*) = 32 )$$

### 問題 12.6.

最適な生産量： $x^* = 4$

$$( R(x) = 2x, \pi(x) = -\frac{1}{3}x^3 + \frac{5}{2}x^2 - 4x - \frac{2}{3}, \pi(x^*) = 2 )$$

## 13 經濟数学入門 I (自習用問題・略解)

### 問題 13.1.

$$(1) (x, y) = (3, 6)$$

$$(2) (x, y) = (4, 4)$$

$$(3) (x, y) = (2, 8)$$

$$(4) (x, y) = (3, 6)$$

### 問題 13.2.

$$(1) (x, y) = \left(\frac{9}{2}, \frac{3}{2}\right)$$

$$(2) (x, y) = (6, 1)$$

$$(3) (x, y) = (3, 2)$$

$$(4) (x, y) = \left(\frac{9}{2}, \frac{3}{2}\right)$$

### 問題 13.3.

$$(1) (x, y) = \left(8, \frac{8}{3}\right)$$

$$(2) (x, y) = \left(4, \frac{16}{3}\right)$$

$$(3) (x, y) = (9, 2)$$

$$(4) (x, y) = (3, 6)$$

### 問題 13.4.

$$(1) (x, y) = (10, 4)$$

$$(2) (x, y) = (5, 8)$$

$$(3) (x, y) = \left(\frac{45}{4}, 3\right)$$

$$(4) (x, y) = \left(\frac{15}{4}, 9\right)$$

## 14 經濟数学入門 I (自習用問題・略解)

### 問題 14.1.

$$(1) \frac{12 - 10}{10} = \frac{1}{5} \quad (20\%)$$

$$(2) \frac{16 - 10}{10} = \frac{3}{5} \quad (60\%)$$

$$(3) \frac{180 - 200}{200} = -\frac{1}{10} \quad (-10\%)$$

$$(4) \frac{120 - 200}{200} = -\frac{2}{5} \quad (-40\%)$$

### 問題 14.2.

$$(1) E = \frac{180 - 200}{12 - 10} \cdot \frac{10}{200} = -\frac{1}{2}$$

$$(2) E = \frac{120 - 200}{12 - 10} \cdot \frac{10}{200} = -2$$

$$(3) E = \frac{180 - 200}{16 - 10} \cdot \frac{10}{200} = -\frac{1}{6}$$

$$(4) E = \frac{120 - 200}{16 - 10} \cdot \frac{10}{200} = -\frac{2}{3}$$

### 問題 14.3.

$$(1) E = \frac{200 - 250}{18 - 15} \cdot \frac{15}{250} = -1$$

$$(2) E = \frac{240 - 250}{18 - 15} \cdot \frac{15}{250} = -\frac{1}{5}$$

$$(3) E = \frac{300 - 250}{12 - 15} \cdot \frac{15}{250} = -1$$

$$(4) E = \frac{350 - 250}{12 - 15} \cdot \frac{15}{250} = -2$$

### 問題 14.4.

$$(1) E(5) = -2 \cdot \frac{5}{20} = -\frac{1}{2} \quad (\text{非弾力的})$$

$$(2) E(6) = -2 \cdot \frac{6}{18} = -\frac{2}{3} \quad (\text{非弾力的})$$

$$(3) E(7) = -2 \cdot \frac{7}{16} = -\frac{7}{8} \quad (\text{非弾力的})$$

$$(4) E(8) = -2 \cdot \frac{8}{14} = -\frac{8}{7} \quad (\text{弾力的})$$

### 問題 14.5.

$$(1) E(5) = -8 \cdot \frac{5}{160} = -\frac{1}{4} \quad (\text{非弾力的})$$

$$(2) E(10) = -8 \cdot \frac{10}{120} = -\frac{2}{3} \quad (\text{非弾力的})$$

$$(3) E(15) = -8 \cdot \frac{15}{80} = -\frac{3}{2} \quad (\text{弾力的})$$

$$(4) E(20) = -8 \cdot \frac{20}{40} = -4 \quad (\text{弾力的})$$