

# Heavy Quarkonium in QGP on the Lattice

Takashi Umeda

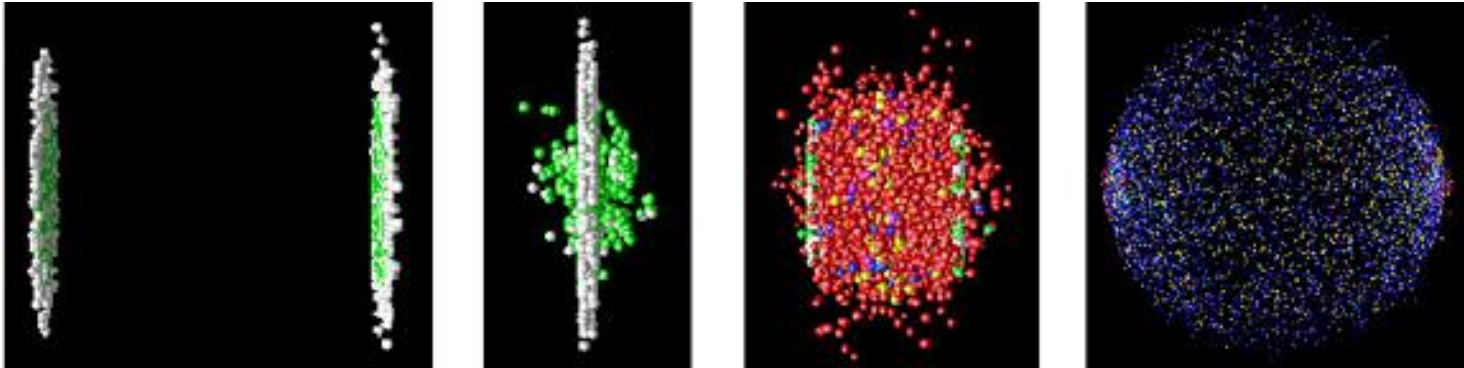


*3rd Asian Triangle Heavy-Ion Conference  
CCNU, Wuhan, China, October 18-20, 2010*

# Contents of this talk

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from the Phenix group web-site



- Introduction

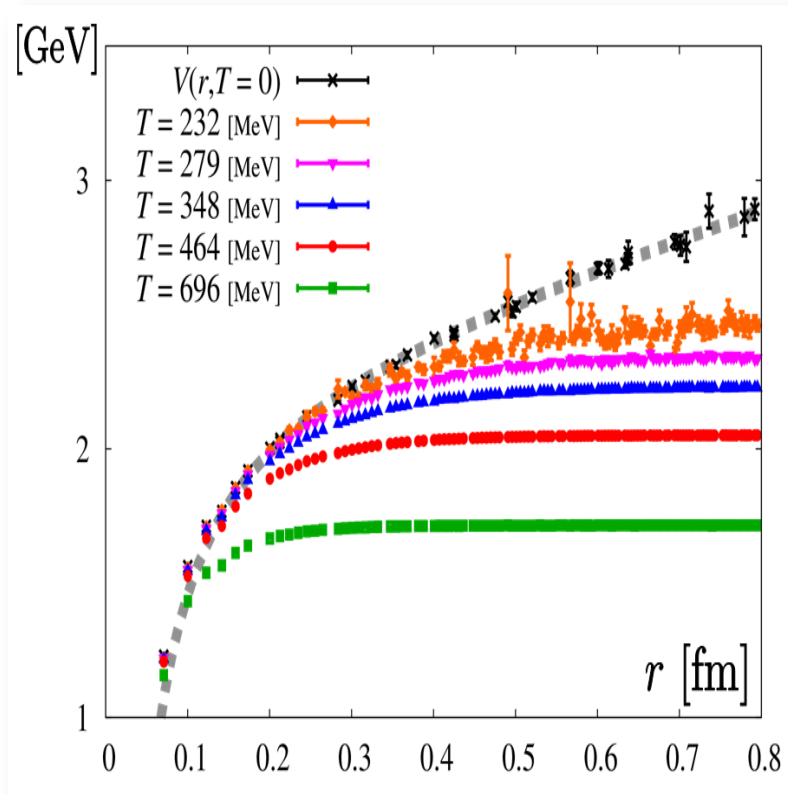
- $J/\psi$  suppression
- Lattice studies with Maximum Entropy Method (MEM)
- Sequential  $J/\psi$  dissociation

- Zero mode contributions

- Other approaches to study charmonium dissociation

- Summary

# J/ $\psi$ suppression as a signal of QGP



Static quark free energy  
WHOT-QCD Collab. ('07)

$N_f=2+1$  QCD result

Confined phase:  
linear raising potential  
→ bound state of  $c - \bar{c}$

De-confined phase:  
Debye screening  
→ scattering state of  $c - \bar{c}$   
( J/ $\psi$  dissociation )

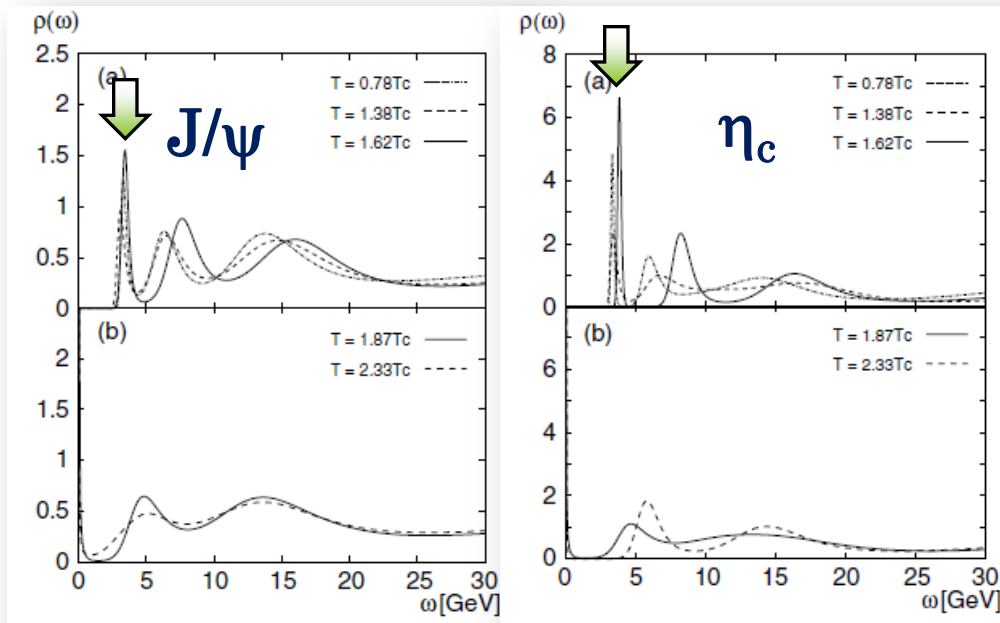
T.Hashimoto et al.('86),  
Matsui&Satz('86)

# Maximum Entropy Method (MEM)

$$G(\tau) = \sum_{\vec{x}, i} \langle J_i(\vec{x}, \tau) J_i^\dagger(\vec{x}, 0) \rangle = \int_0^\infty d\omega \frac{e^{-\omega\tau}}{1 - e^{-\frac{\omega}{T}}} \rho(\omega)$$

Charmonium correlator on the lattice

Spectral function (SPF)



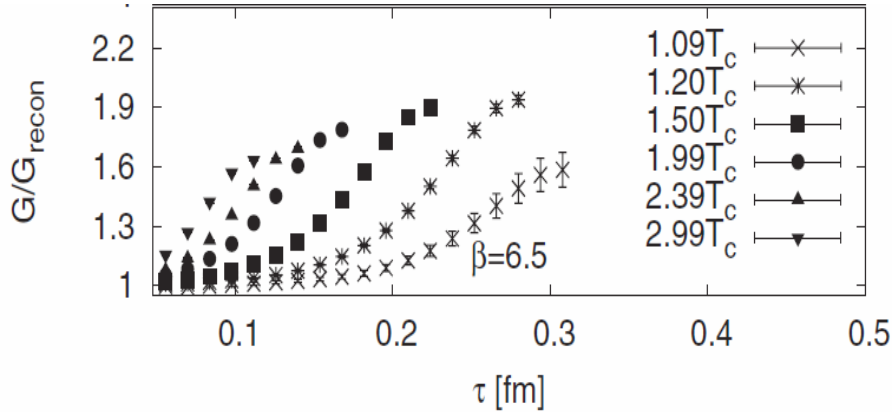
Charmonium spectral func.  
Asakawa & Hatsuda ('04)

Quench QCD ( $N_f=0$ )

Maximum Entropy Method

$J/\psi$  &  $\eta_c$   
survive till  $1.62 T_c$   
dissociate at  $1.87 T_c$

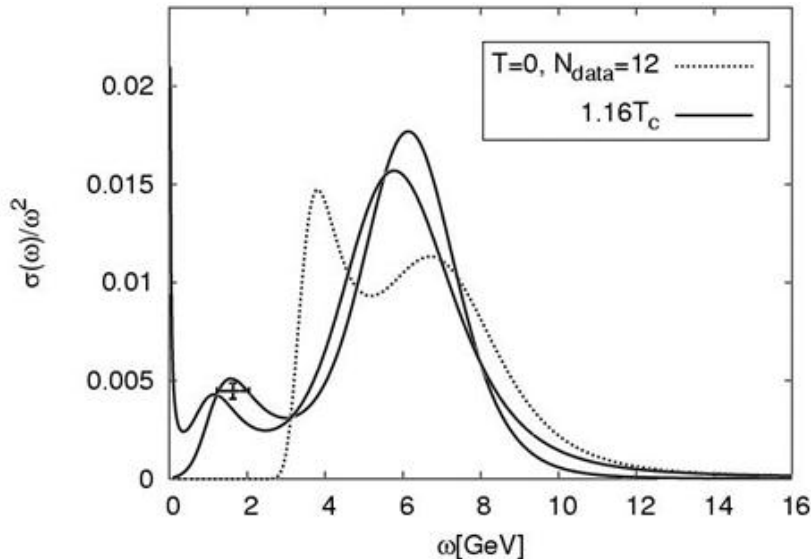
# P-wave states ( $\chi_c$ ) in charmonium



## Results on P-wave states

A.Jakovac et al. ('07)

$G_{\text{recon}}$  is a charmonium correlator constructed with SPF at  $T=0$ .  
 No change in SPF at  $T>0$   
 leads to  $G/G_{\text{recon}} = 1$



- Drastic change in  $\chi_c$  correlator above  $T_c$

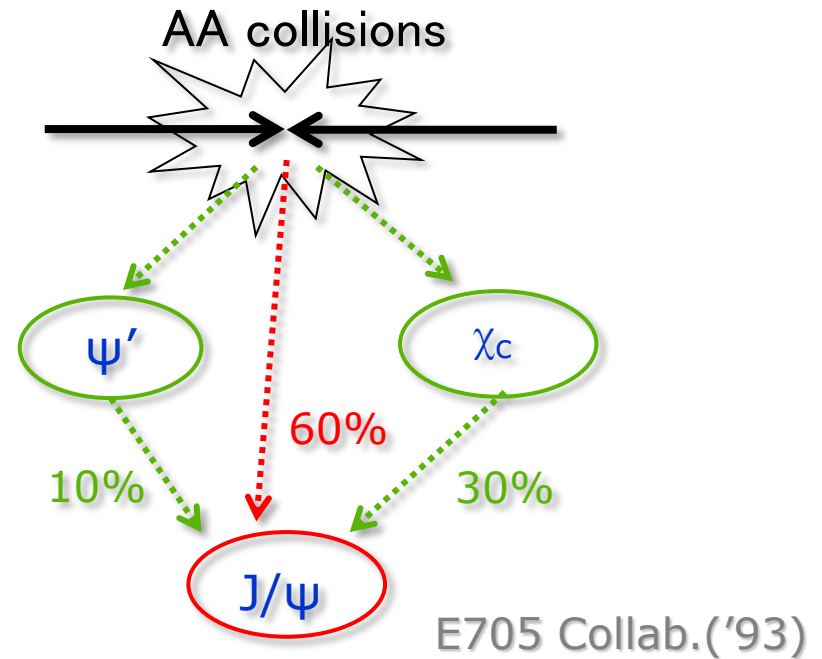
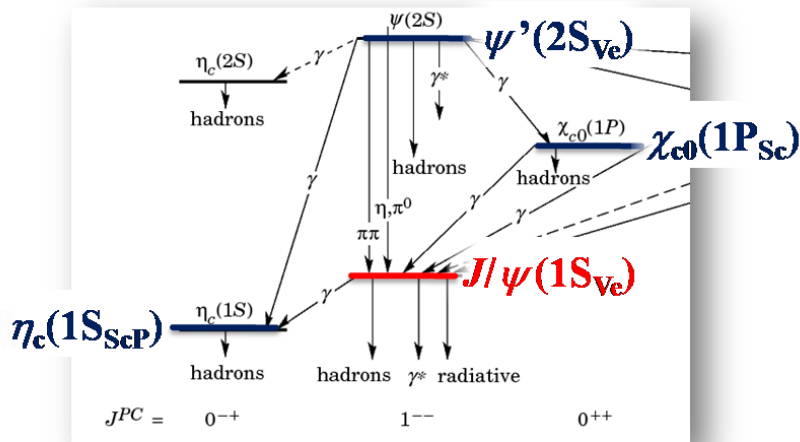
- MEM results indicate  $\chi_c$  dissociation just above  $T_c$  (?)

“Default model” is  
 input information for MEM analysis  
 Default model dependence is  
 one of systematic errors

# Possible $J/\psi$ suppression scenario

## Sequential charmonium dissociation

F. Karsch et al. ('05)

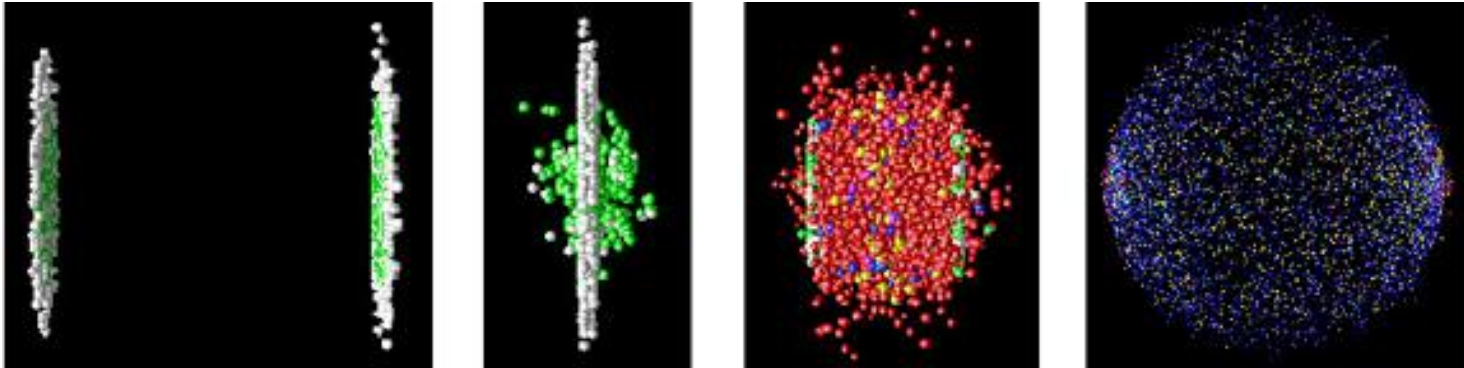


When  $\chi_c$  or/and  $\psi'$  dissociate just above  $T_c$ ,  
part of  $J/\psi$  suppression occurs  
even if  $J/\psi$  survives in QGP.

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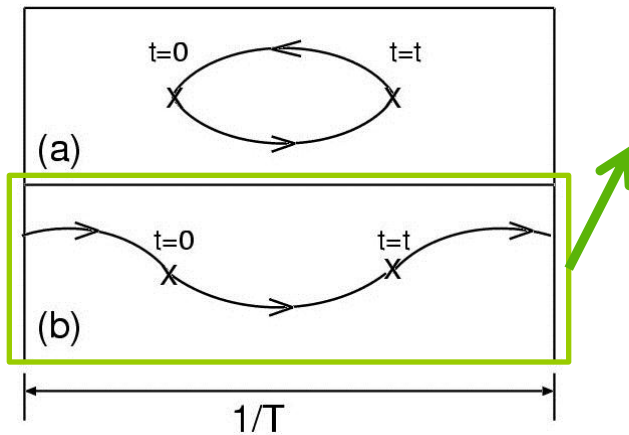
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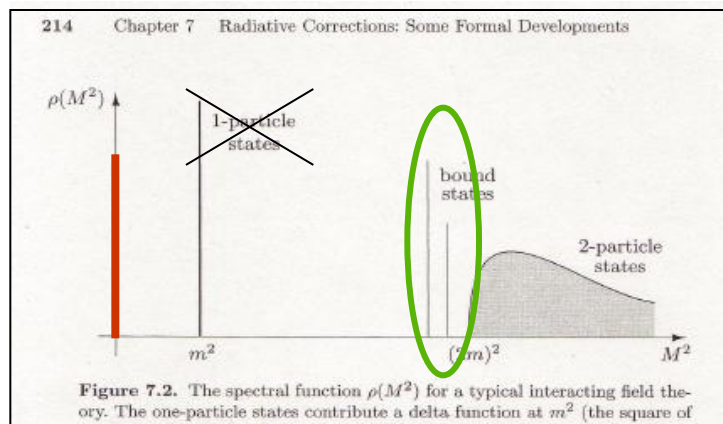
# Zero mode in meson correlators



$$\exp(-m_q t) \times \exp(-m_q(L_t - t)) = \frac{\exp(-m_q L_t)}{\text{zero mode}}$$

$L_t = 1/T =$  temporal extent  
 $m_q$  is single quark energy

T. Umeda ('07)



"An Introduction to Quantum Field Theory"  
 Michael E. Peskin, Perseus books (1995)

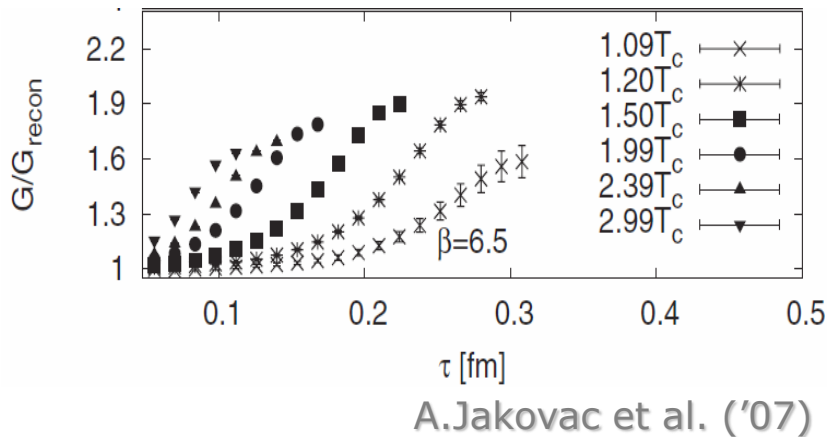
- The zero mode is part of Landau dumping but it is not relevant whether charmonium dissociates or survives.
- One can remove the zero mode effects by derivative of correlators

$$G(\tau)/G_{recon}(\tau) \longrightarrow G'(\tau)/G'_{recon}(\tau)$$

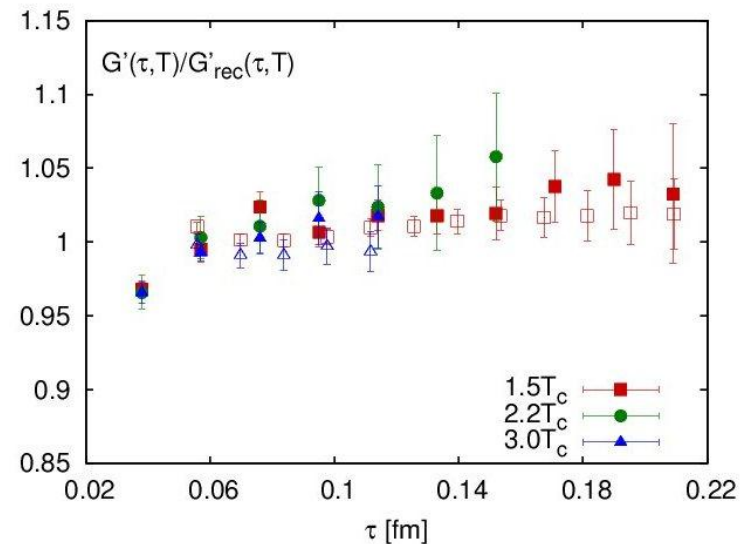


# Zero mode in meson correlators

Spectral changes in  $\chi_{c0}$   
w/ zero mode



w/o zero mode



- The drastic change of correlators is due to the zero mode
- No change in  $\chi_c$  SPF within statistical errors

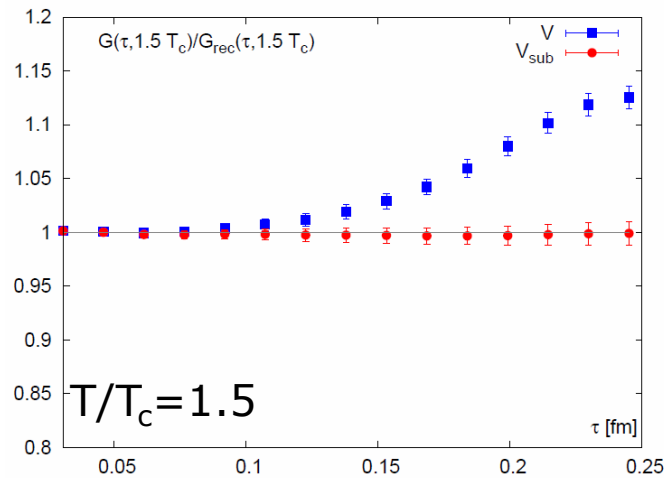
$G_{\text{recon}}$  is a charmonium correlator constructed with SPF at  $T=0$ .  
No change in SPF at  $T>0$  leads to  $G/G_{\text{recon}} = 1$

# J/ψ results taking account of zero mode

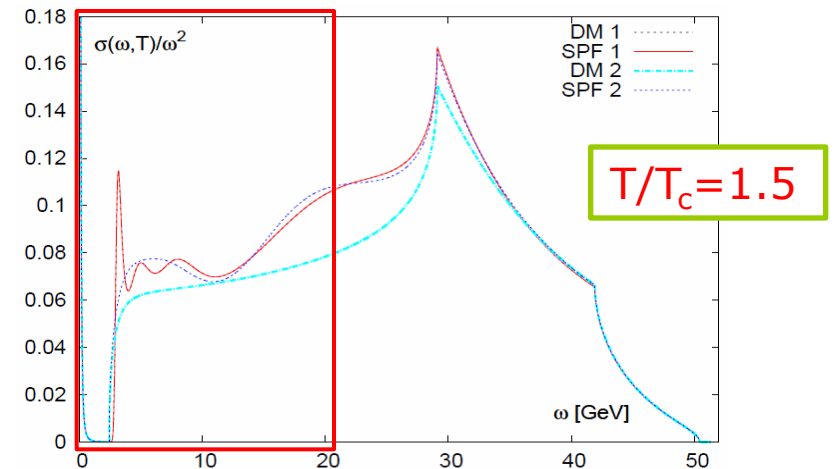
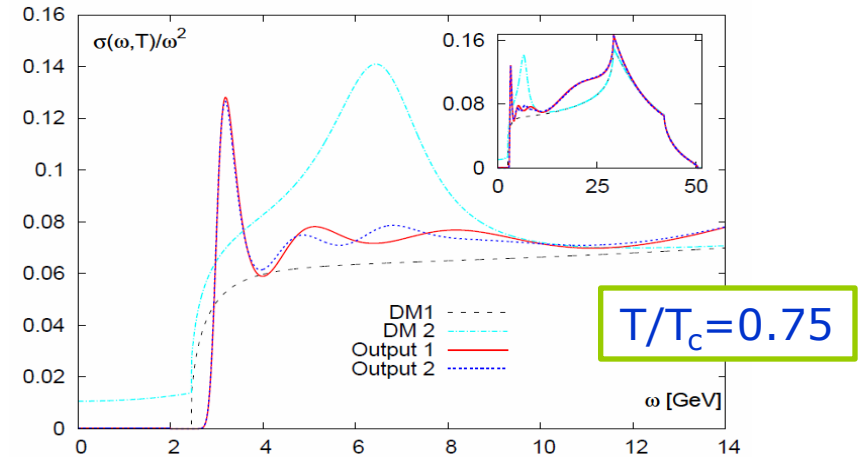
## Zero mode in J/ψ correlator

H.Ding et al. ('09)

Spectral changes in J/ψ  
w/ & w/o zero mode



No change in J/ψ SPF  
within statistical error

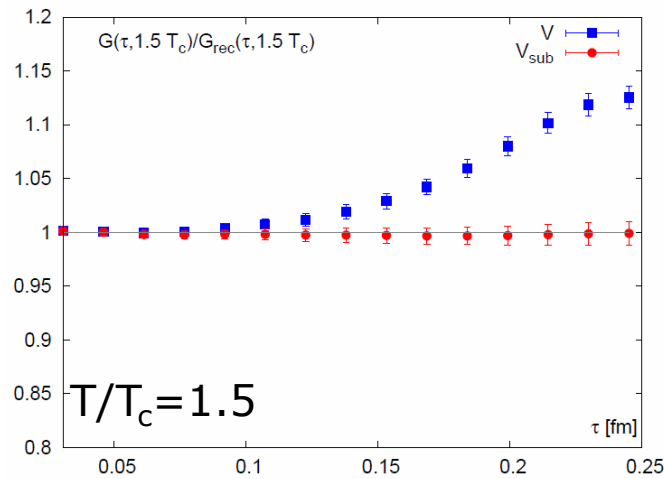


# J/ $\psi$ results taking account of zero mode

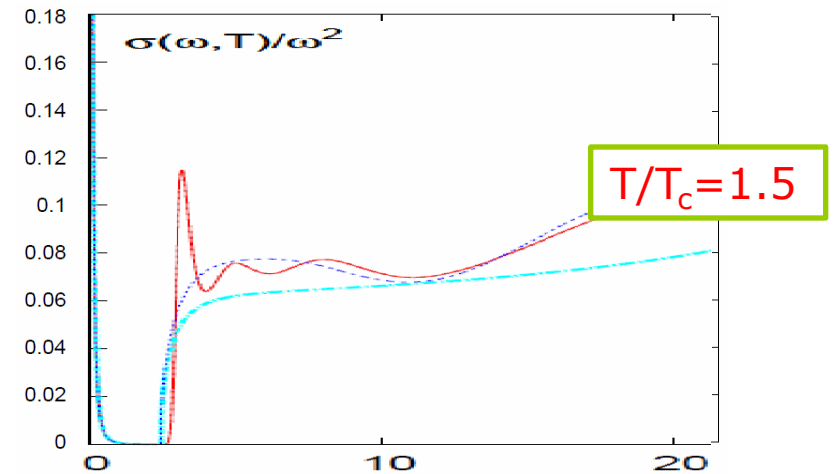
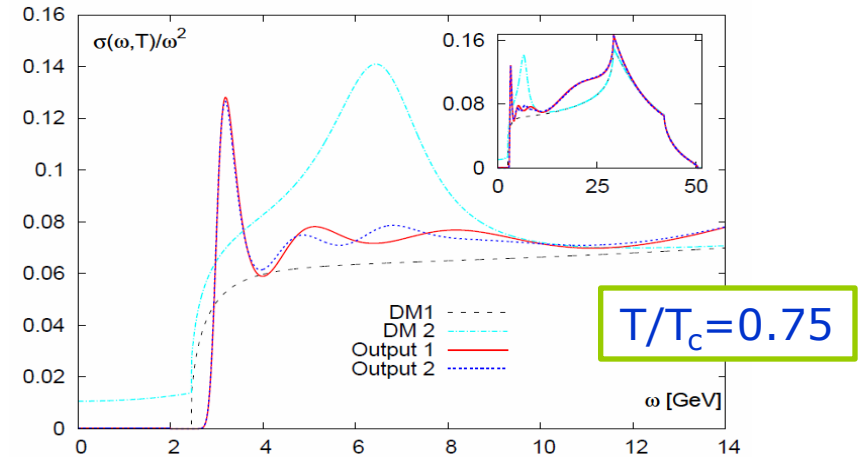
## Zero mode in J/ $\psi$ correlator

H.Ding et al. ('09)

Spectral changes in J/ $\psi$   
w/ & w/o zero mode

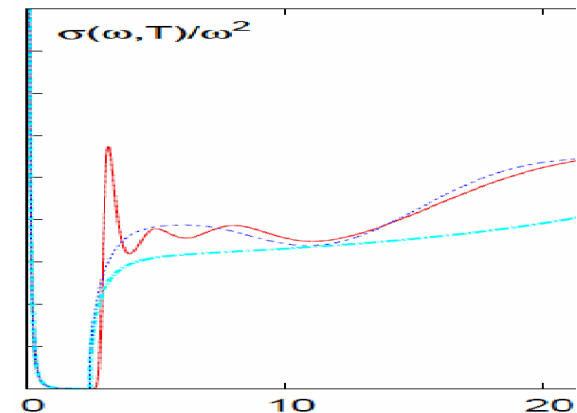
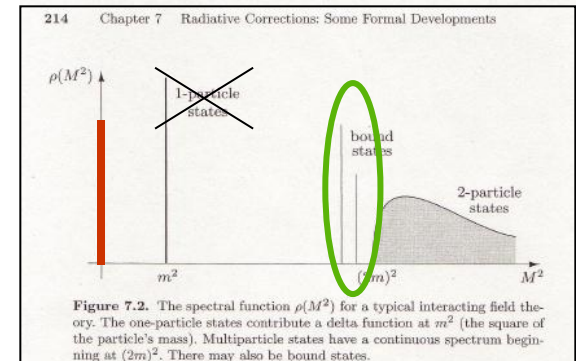


No change in J/ $\psi$  SPF  
within statistical error



# Zero mode & MEM results

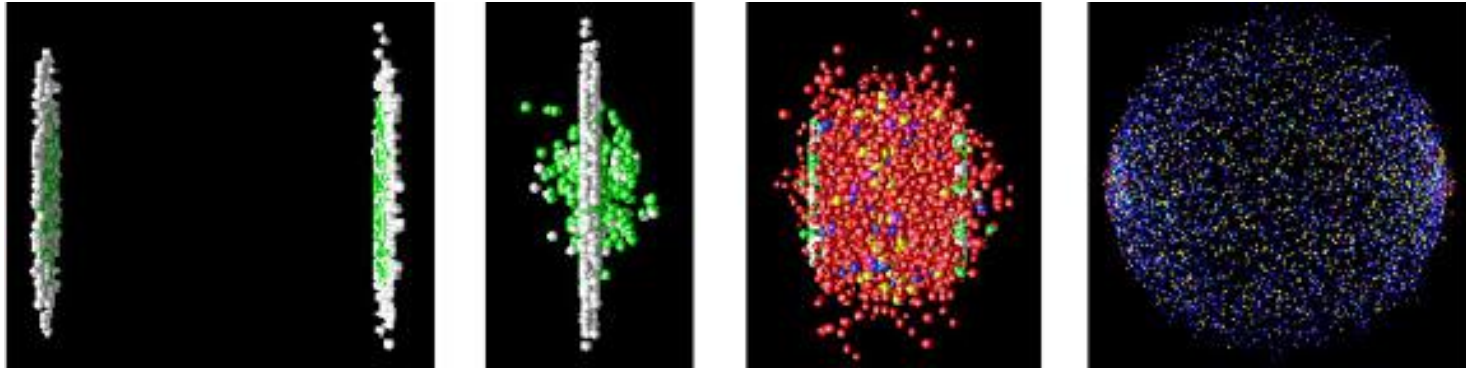
- **No significant change** in correlators at  $T > 0$  except for the zero mode effect.
- Zero mode is not relevant to charmonium dissociations.
- The default model is necessary in MEM analysis. No good default model for charmonium SPFs.  
**default model dependence**  
→ a systematic error in MEM
- T. Ding et al. ('09) shows that **both SPFs w/ & w/o  $J/\psi$  peak** can be extracted from **common charmonium correlator** at  $1.5T_c$  by MEM.



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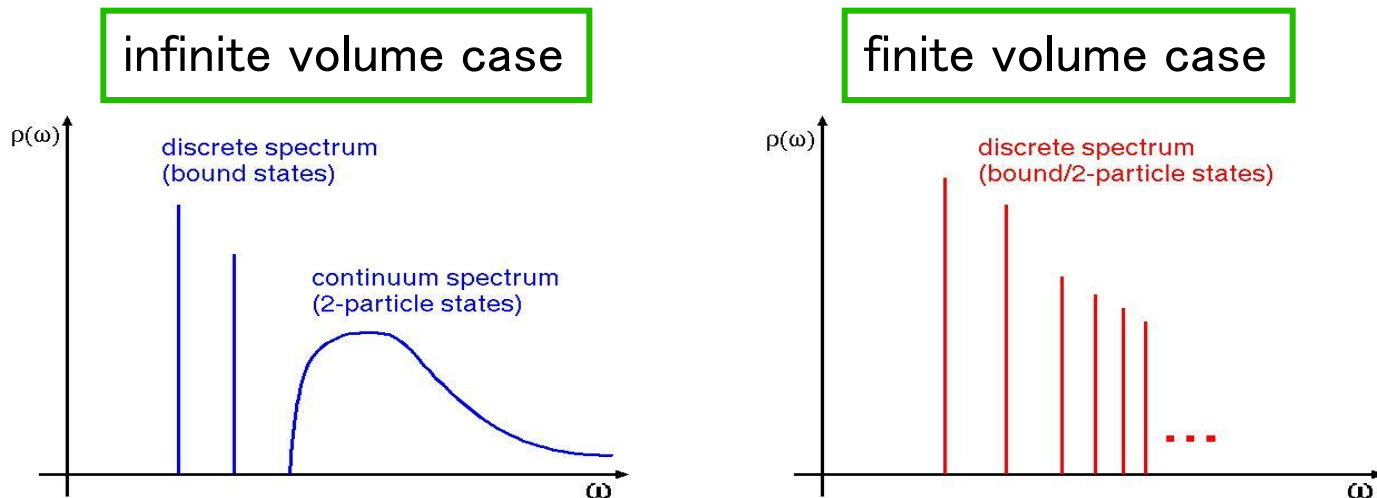
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# Spectral functions in a finite volume

Momenta are discretized in finite ( $V=L^3$ ) volume

$p_i/a = 2n_i\pi/L$  ( $n_i=0, \pm 1, \pm 2, \dots$ ) for Periodic boundary condition

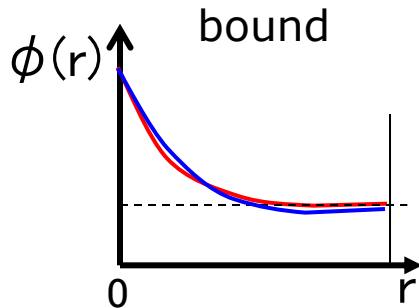


In a finite volume (e.g. Lattice simulations),  
discrete spectra does not always indicate bound states !

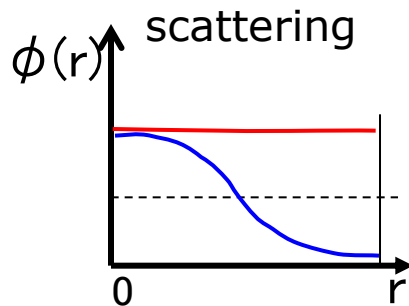
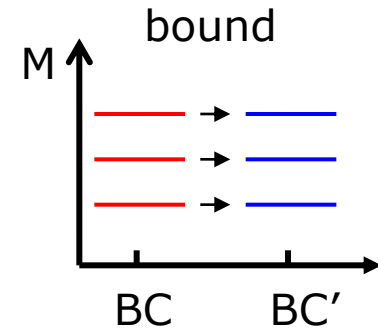
# Other approaches to study charmonium dissociation

## Quark boundary conditions (B.C.) in space (finite volume on the lattice)

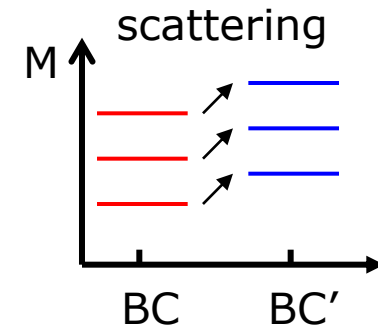
H. Iida et al. ('06)



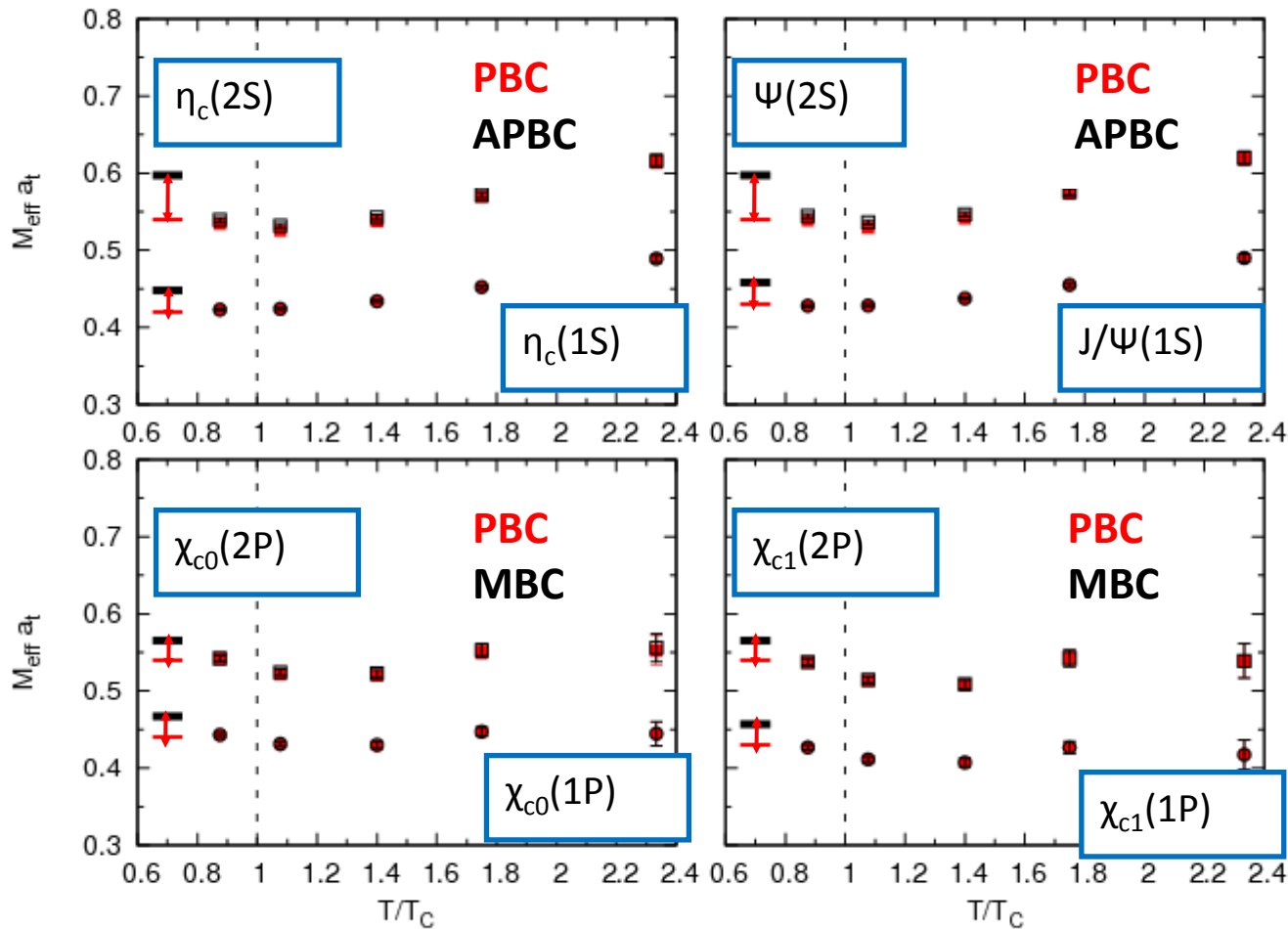
The wave functions are localized,  
their energies are insensitive to B.C.



The momenta depends on BC,  
the scattering state energies  
are sensitive to B.C.



# Charmonium spectra in various boundary conditions



$$q(x_i + L_i) = b_i q(x_i)$$

$b_i = 1$  : periodic  
 $b_i = -1$  : anti-periodic

**PBC** :  $b=(1, 1, 1)$   
**APBC** :  $b=(-1, -1, -1)$   
**MBC** :  $b=(-1, 1, 1)$

an expected gap  
 in  $V=(2\text{fm})^3$   
 (free quark case)  
 $\sim 200\text{MeV}$

■ No significant differences in the different B.C.

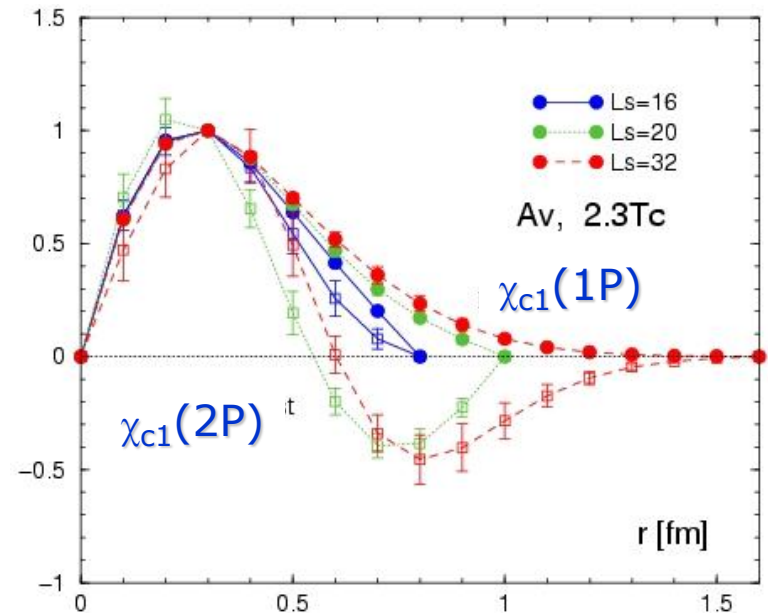
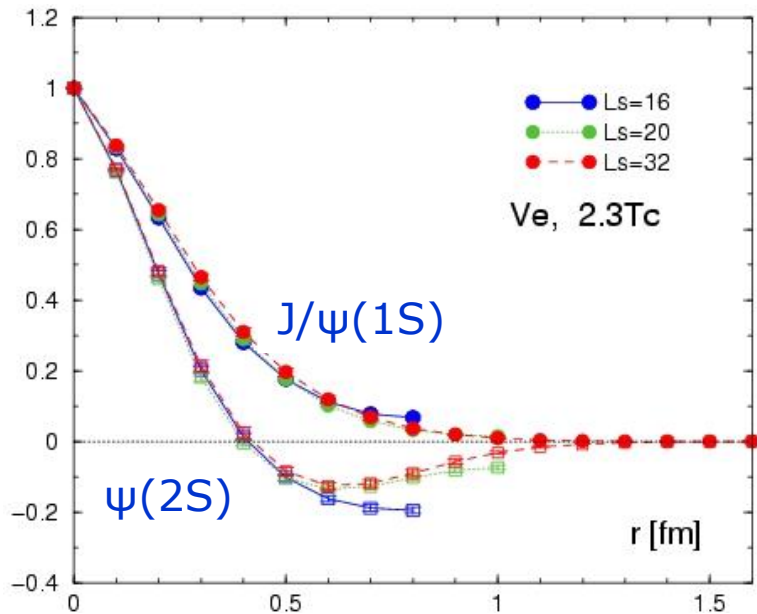
H. Ohno et al. ('08)



# Charmonium wave function on the lattice

(Bethe-Salpeter) "Wave function" at  $T=2.3T_c$

H. Ohno et al. ('08)



■ Clear signals of bound states even at  $T=2.3T_c$

# Summary on lattice studies of charmonium dissociations

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- Because of MEM results on the lattice,
  - $J/\psi$  state survives till  $1.5T_c$  or more and, dissociates around  $1.5-2.0T_c$
  - $\chi_c$  states dissociate just above  $T_c$are widely believed.
- Analysis taking the zero mode into account
  - No significant spectral changes in QGP (except for zero mode)
- MEM results include large default model dependence
- Other approaches to study charmonium dissociation indicate no clear signal of dissociation

# Summary and Outlook

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- Puzzle of  $J/\psi$  suppression in QGP  
     $J/\psi$  should dissociate at very high temperature because of the asymptotic freedom.
- Lattice QCD has never seen such evidences yet (except for MEM).  
    High temperature calculations are time consuming on the lattice.
- Non-MEM studies at very high temperature ( $T/T_c=3\sim 5$ ) are desired.

Thank you for your attention !

# Buckup slides

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# Wave functions at finite temperature

Temp. dependence of ( Bethe-Salpeter ) "Wave function"

$$BS(\vec{r}, t) = \sum_{\vec{x}} \langle \bar{q}(\vec{x} + \vec{r}, t) \Gamma q(\vec{x}, t) \bar{q}(\vec{0}, 0) \Gamma q(\vec{0}, 0) \rangle$$

$$\Psi(|\vec{r}|, t) = BS(\vec{r}, t) / BS(\vec{r}_0, t)$$

$$\Gamma = \begin{cases} \gamma_5 & (\text{Ps}) \\ \gamma_i & (\text{Ve}) \quad (i = 1, 2, 3) \\ \sum_j \left( \vec{\partial}_j \gamma_j - \overleftarrow{\partial}_j \gamma_j \right) & (\text{Sc}) \\ \sum_{j,k} \epsilon_{ijk} \left( \vec{\partial}_j \gamma_k - \overleftarrow{\partial}_j \gamma_k \right) & (\text{Av}) \quad (i = 1, 2, 3) \end{cases}$$

using the eigen functions of the variational method  
→ we can extract the wave functions of each states

# Summary and future plan

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We investigated  $T_{\text{dis}}$  of charmonia from Lattice QCD using another approach to study charmonium at  $T > 0$  without Bayesian analysis

- boundary condition dependence
- Wave function (Volume dependence)

No evidence for unbound c-c quarks up to  $T = 2.3 T_c$

→ The result may affect the scenario of  $J/\psi$  suppression.

## Future plan

- Interpretations of the experimental results on  $J/\psi$  suppression
- Higher Temp. calculations (  $T/T_c = 3 \sim 5$  )
- Full QCD calculations (  $N_f = 2+1$  Wilson is now in progress )

# Maximum Entropy Method (MEM)

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## Other lattice studies:

T.Umeda et al.('02), S.Datta et al.('04),  
Asakawa&Hatsuda('04), A.Jakovac et al.('07), G.Aatz et al.('06)

→ all calculations conclude that  $J/\psi$  survives till  $1.5T_c$  or higher